

Q1.

Fully destructive interference between two identical sinusoidal waves occurs only if they:

- A) travel in the same direction and are 180° out of phase
- B) travel in opposite directions and are 180° out of phase
- C) travel in the same direction and are in phase
- D) travel in opposite directions and are in phase
- E) travel in the same direction and are 90° out of phase

Ans:

A

Q2.

A 4.00-m long string, clamped at both ends, vibrates at 200 Hz. If the string resonates in six loops, what is the speed of transverse waves on the string?

- A) 267 m/s
- B) 133 m/s
- C) 100 m/s
- D) 328 m/s
- E) 400 m/s

Ans:

$$1 \text{ loop} = \frac{\lambda}{2}$$

$$\therefore 6 \text{ loops} = 3\lambda = L$$

$$\Rightarrow \lambda = \frac{L}{3} = \frac{4}{3} \text{ m}$$

$$\therefore V = f\lambda = 200 \times \frac{4}{3} = 267 \text{ m/s}$$

Q3.

A string of linear mass density 64 g/m is stretched under tension of magnitude 40 N. A wave is traveling along the string with a frequency of 120 Hz and amplitude of 8.0×10^{-3} m. What is the average rate of energy that must be supplied by a generator to produce this wave in the string?

- A) 29 W
- B) 3.6 W
- C) 0.73 W
- D) 0.24 W
- E) 15 W

Ans:

$$P = \frac{1}{2} \mu \omega^2 y_m^2 v; \quad v = \sqrt{\frac{\tau}{\mu}}$$
$$\mu = 64 \times 10^{-3} \text{ kg/m}, \quad \tau = 40 \text{ N}, \quad y_m = 8 \times 10^{-3} \text{ m}$$
$$f = 120 \text{ Hz} \Rightarrow \omega = 2\pi f = 240 \pi \text{ rad/s}$$
$$\Rightarrow P = 29 \text{ W}$$

Q4.

Which of the following answers is the correct equation of a wave traveling along negative x-axis with a speed of 220 m/s, frequency 70 Hz and amplitude 0.025 m? (x is in meters and t is in seconds).

- A) $y = 0.025 \sin(2.0 x + 440 t)$
- B) $y = 0.025 \sin(2.0 x - 440 t)$
- C) $y = 0.025 \sin(3.1 x + 70 t)$
- D) $y = 0.025 \sin(3.1 x - 70 t)$
- E) $y = 0.025 \sin(2.5 x + 220 t)$

Ans:

$$\omega = 2\pi f = 2\pi \times 70 = 440$$
$$k = \frac{2\pi}{\lambda} \quad (v = f\lambda) = \frac{2\pi f}{v} = \frac{440}{220} = 2$$

Q5.

Sound waves travel at 343 m/s in air and at 1500 m/s in water. A 256-Hz sound wave is generated inside a pool of water, and you hear the sound standing beside the pool. In the air,

- A) the frequency of the sound is the same, but its wavelength is shorter.
- B) the frequency of the sound is higher, but its wavelength stays the same.
- C) the frequency of the sound is lower, and its wavelength is longer.
- D) the frequency of the sound is lower, and its wavelength is shorter.
- E) both the frequency and the wavelength of the sound stay the same.

Ans:

$$\lambda = \frac{v}{f}, \quad f \text{ is constant}$$

Q6.

A car moving at 40.0 m/s approaches a stationary whistle that emits a 200 Hz sound. The speed of sound in air is 343 m/s. What is the frequency of the sound heard by the driver of the car?

- A) 223 Hz
- B) 200 Hz
- C) 177 Hz
- D) 179 Hz
- E) 226 Hz

Ans:

$$f' = f \left(\frac{v + v_D}{v - v_S} \right)$$

$$v_S = 0, v_D = 40, v = 343, f = 200$$

$$\Rightarrow f' = 223 \text{ Hz}$$

Q7.

Consider an organ pipe A with both ends open and an organ pipe B with one end open. The third harmonic of B has the same frequency as the second harmonic of A. What is the ratio of their lengths, L_A/L_B ?

- A) 1.3
- B) 0.75
- C) 1.0
- D) 2.0
- E) 0.50

Ans:

$$\text{For pipe A: } f_n = \frac{nv}{2L}$$

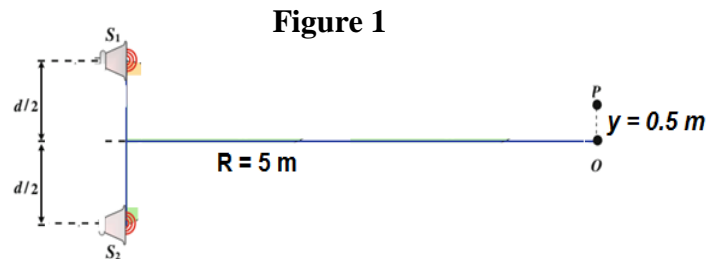
$$\text{For pipe B: } f_n = \frac{nv}{4L}$$

$$\text{Given that } 2 \cdot \frac{v}{2L_A} = 3 \cdot \frac{v}{4L_B} \Rightarrow \frac{L_A}{L_B} = \frac{4}{3} = 1.3$$

Q8.

Two identical speakers, S_1 and S_2 , are placed 2 m apart, as shown in **Figure 1**, and emit sound waves driven by the same oscillator. A listener is originally located at point O, which is a distance $R = 5$ m from the center of the line connecting the two speakers. The listener walks to point P, which is a distance $y = 0.5$ m above O, and hears the first minimum in sound intensity. Find the wavelength of the sound wave.

- A) 0.4 m
- B) 0.2 m
- C) 0.5 m
- D) 1 m
- E) 5 m



Ans:

$$\text{First minimum} \Rightarrow S_2P - S_1P = \frac{\lambda}{2}$$

$$S_2P = \sqrt{R^2 + \left(\frac{d}{2} + y\right)^2} = 5.22, \quad S_1P = \sqrt{R^2 + \left(\frac{d}{2} - y\right)^2} = 5.02$$

$$\Rightarrow \lambda = 2(5.22 - 5.02) = 0.4 \text{ m}$$

Q9.

Two metal rods of identical dimensions (length 20.0 cm and cross-sectional area 14.0 cm^2 each) are welded end to end, as shown in **Figure 2**. $T_1 = 0^\circ\text{C}$ and $T_2 = 100^\circ\text{C}$. The thermal conductivities of the rods are $k_1 = 109 \text{ W/m.K}$ and $k_2 = 401 \text{ W/m.K}$. Find the conduction rate through the rods when steady state is reached:

- A) 60.0 W
- B) 25.5 W
- C) 120 W
- D) 30.0 W
- E) 42.9 W



Ans:

$$\text{At steady state } k_1 \frac{A}{L} (T - T_1) = \frac{Q}{t} = k_2 \frac{A}{L} (T_2 - T)$$

(where T is the temperature at the interface)

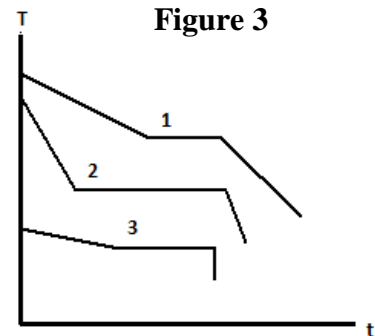
$$\Rightarrow T = 351.6 \text{ K}$$

$$\therefore \frac{Q}{t} = k_1 \frac{A}{L} (T - T_1) = 60 \text{ W}$$

Q10.

Three different materials of identical mass are placed one at a time in a special freezer that can extract energy from the material at a certain constant rate. During the cooling process, each material begins in the liquid state and ends in the solid state; **Figure 3** shows the temperature T versus time t . Rank the materials according to their specific heat in the liquid state, greatest first.

- A) 3, 1, 2
- B) 3, 2, 1
- C) 1, 2, 3
- D) 1, 3, 2
- E) 2, 3, 1



Ans:

$$\frac{Q}{t} = \frac{mc\Delta T}{t} = \text{constant}$$

$$\Rightarrow c \cdot \frac{\Delta T}{t} = \text{constant}$$

$$\frac{\Delta T}{t} = \text{slope of } T \text{ vs } t \text{ graph}$$

High temperature portion of the graph represents liquid state.

Slope of 2 > slope of 1 > slope of 3

$$\Rightarrow c_2 < c_1 < c_3$$

Q11.

What is the minimum amount of energy required to completely melt 150 g of silver initially at 298 K? (For Silver: Specific heat = 236 J/kg.K, Melting point = 1235 K, Heat of fusion = 105 kJ/kg)

- A) 48.9 kJ
- B) 58.6 kJ
- C) 33.2 kJ
- D) 15.8 kJ
- E) 42.8 kJ

Ans:

$$Q = mc\Delta T + mL_F = 48.9 \text{ kJ}$$

Q12.

A thermodynamic system undergoes a process in which its internal energy decreases by 600 J. At the same time, 250 J of work is done on the system. The heat energy to the system is

- A) -850 J
- B) +350 J
- C) +850 J
- D) -350 J
- E) 0 J

Ans:

$$\begin{aligned} Q &= W + \Delta E_{\text{int}} \\ &= (-250) + (-600) \\ &= -850 \text{ J} \end{aligned}$$

Q13.

Variation of Pressure with Volume of an ideal gas at constant temperatures T_1 and T_2 is represented by two isotherms shown in **Figure 4**. Internal energy of the gas is denoted by E_{int} . Which of the following is true?

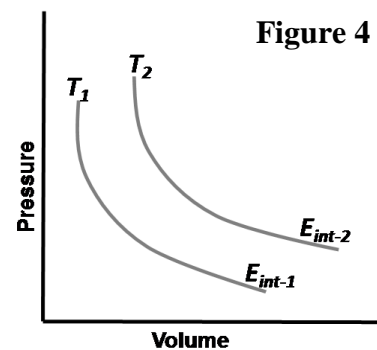
- A) $E_{\text{int-1}} < E_{\text{int-2}}$
- B) $T_1 > T_2$
- C) $T_1 = T_2$
- D) $E_{\text{int-1}} > E_{\text{int-2}}$
- E) $E_{\text{int-1}} = E_{\text{int-2}}$

Ans:

$$E_{\text{int}} \propto T$$

From the graph $T_1 < T_2$

$$\therefore E_{\text{int-1}} < E_{\text{int-2}}$$



Q14.

An ideal gas is enclosed in a cylinder. If the temperature of the gas is increased from 100 °C to 200 °C at constant volume, the pressure of the gas will change from P to

- A) 1.27 P
- B) 2.00 P
- C) 3.00 P
- D) 0.500 P
- E) 1.50 P

Ans:

Constant V

$$\therefore \frac{P_1}{T_1} = \frac{P_2}{T_2}$$

$$T_1 = 273 + 100 = 373 \text{ K}$$

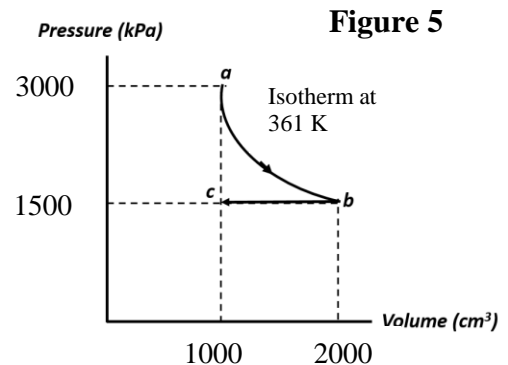
$$T_2 = 273 + 200 = 473 \text{ K}$$

$$\Rightarrow \frac{P_2}{P_1} = \frac{T_2}{T_1} = 1.27$$

Q15.

One mole of ideal gas goes from initial state 'a' to final state 'c' as shown in **Figure 5**, where *ab* is isotherm at 361.0 K and *bc* is isobaric at 1500 kPa. Find the total work done by the gas along the path *abc*.

- A) 579.4 J
- B) 2079 J
- C) 3579 J
- D) 1500 J
- E) 9000 J



Ans:

$$W_{abc} = W_{ab} + W_{bc}$$

$$= nRT \ln \left(\frac{V_f}{V_i} \right) + P \cdot \Delta v$$

$$= 1 \times 8.31 \times 361 \ln(2) + 1500 \times 10^3 \times (1000 - 2000) \times 10^{-6} = 579.4 \text{ J}$$

Q16.

When 20.9 J was added as heat to an ideal gas, its volume changed from 50.0 cm³ to 100 cm³ while its pressure remained at 1.00 atm. The C_p of the gas is

- A) 34.4 J/mol.K
- B) 17.2 J/mol.K
- C) 20.9 J/mol.K
- D) 50.0 J/mol.K
- E) 25.0 J/mol.K

Ans:

$$Q = nc_p \Delta T = n c_p \cdot \frac{P \Delta V}{nR}$$

$$\Rightarrow c_p = \frac{QR}{P \Delta V} = 34.4 \text{ J mol. K}$$

Q17.

You wish to increase the coefficient of performance of an ideal refrigerator that works between temperatures T_L and T_H. Which of the following (assume that the slight increase or decrease in T_L or T_H is the same in all answers) would give the greatest increase?

- A) Running the cold reservoir at slightly higher temperature.
- B) Running the cold reservoir at slightly lower temperature.
- C) Moving the refrigerator to a slightly warmer room.
- D) Moving the refrigerator to a slightly cooler room.
- E) Restarting the refrigerator.

Ans:

$$K = \frac{Q_L}{W} = \frac{Q_L}{Q_H - Q_L}$$
$$= \frac{T_L}{T_H - T_L}$$

Q18.

The efficiency of a car engine is 20 % when the engine does 6.0 kJ of work per cycle. Assume the process is reversible. After a tune-up, the efficiency increased to 30 %. By how much the energy lost is reduced for the same amount of work?

- A) 10 kJ
- B) 12 kJ
- C) 20 kJ
- D) 16 kJ
- E) 18 kJ

Ans:

$$\begin{aligned}\varepsilon &= \frac{W}{Q_H} = \frac{W}{Q_L + W} \Rightarrow Q_L = W \left(\frac{1}{\varepsilon} - 1 \right) \\ \Rightarrow Q_{L1} &= 6 \left(\frac{1}{0.2} - 1 \right) = 24 \text{ kJ} \\ Q_{L2} &= 6 \left(\frac{1}{0.3} - 1 \right) = 14 \text{ kJ} \\ \therefore Q_{L1} - Q_{L2} &= 10 \text{ kJ}\end{aligned}$$

Q19.

A 20-g ice cube at -10°C is dropped in a lake whose temperature is 15°C . Calculate the change in entropy of the lake as the ice cube comes to thermal equilibrium with the lake. Specific heat of ice = 2220 J/kg.K, and the effect of ice cube on the lake's temperature is negligible.

- A) -29 J/K
- B) +29 J/K
- C) +31 J/K
- D) -31 J/K
- E) 0

Ans:

$$\begin{aligned}\Delta S &= \frac{\Delta Q}{T} = -[mc_{\text{ice}}(0 - (-10)) + mL_f + mc_{\text{water}}(15 - 0)] / (273 + 15) \\ &= -29 \text{ J/K}\end{aligned}$$

Q20.

Figure 6 represents a Carnot engine that works between temperatures $T_1 = 500$ K and $T_2 = 250$ K, and drives a Carnot refrigerator that works between temperatures $T_3 = 350$ K and $T_4 = 250$ K. What is the ratio Q_3/Q_1 ?

- A) 1.75
- B) 1.25
- C) 1.67
- D) 1.43
- E) 3.50

Ans:

$$\frac{Q_1}{Q_2} = \frac{T_1}{T_2} = 2 \Rightarrow Q_2 = \frac{1}{2}Q_1$$

$$\frac{Q_3}{Q_4} = \frac{T_3}{T_4} = \frac{7}{5} \Rightarrow Q_4 = \frac{5}{7}Q_3$$

$$Q_1 - Q_2 = W = Q_3 - Q_4$$

$$\Rightarrow \frac{1}{2}Q_1 = \frac{2}{7}Q_3 \Rightarrow \frac{Q_3}{Q_1} = \frac{7}{4} = 1.75$$

