

Q1.

A transverse wave on a string with a linear density of 0.200 kg/m is described by the following equation: $y = 0.005 \sin(419 t - 21.0 x)$, where x and y are in meters and t is in seconds. What is the tension in the string?

- A) 79.6 N
- B) 3.99 N
- C) 42.1 N
- D) 32.5 N
- E) 65.8 N

Ans:

$$v = \frac{\omega}{k} = \frac{419}{21.0}$$

$$v = \sqrt{\frac{\tau}{\mu}}$$

$$\Rightarrow v = \mu v^2$$

$$\therefore \tau = 0.200 \times \left(\frac{419}{21.0}\right)^2 = 79.6 \text{ N}$$

Q2.

A stone is dropped into a lake; and it produces circular surface waves with a frequency of 0.25 Hz. When should a second stone be dropped, after the first, at the same place to produce destructive interference? Ignore the time it takes the stone to reach water.

- A) 2.0 s
- B) 1.0 s
- C) 0.75 s
- D) 0.50 s
- E) 1.5 s

Ans:

$$f = \frac{1}{4} \text{ Hz} \rightarrow T = \frac{1}{f} = 4 \text{ s}$$

$$\left. \begin{array}{l} 2\pi \rightarrow T \\ \phi \rightarrow t \end{array} \right\} \rightarrow t = \frac{\phi \cdot T}{2\pi} = \frac{\pi \cdot T}{2\pi} = \frac{T}{2} = 2.0 \text{ s}$$

Q3.

Which one of the following statements is **TRUE** concerning the points on a string that sustains a standing wave pattern?

- A) The amplitude of oscillation is not the same for all points.
- B) All points vibrate vertically with the same speed.
- C) All points undergo the same displacements.
- D) All points vibrate with different frequencies.
- E) Some points undergo motion that is purely longitudinal.

Ans:

A

Q4.

A string with a length of 2.5 m, fixed at both ends, has two successive resonances at frequencies of 112 Hz and 140 Hz. Determine the wavelength of the 140 Hz resonance.

- A) 1.0 m
- B) 0.50 m
- C) 2.0 m
- D) 0.75 m
- E) 1.5 m

Ans:

$$f_1 = \Delta f = 140 - 112 = 28 \text{ Hz}$$

$$f_n = nf_1 \Rightarrow n = \frac{f_n}{f_1} = \frac{140}{28} = 5$$

$$\lambda_n = \frac{2L}{n} = \frac{2 \times 2.5}{5} = 1.0 \text{ m}$$

Q5.

Two transmitters, S1 and S2, shown in **Figure 1**, emit identical sound waves at a frequency of 680 Hz. The transmitters are separated by a distance of 2.0 m. Consider a big circle of radius R with its center halfway between these transmitters. How many interference minima are there on this big circle? Take the speed of sound in air to be 340 m/s.

- A) 16
- B) 4
- C) 8
- D) 3
- E) 12

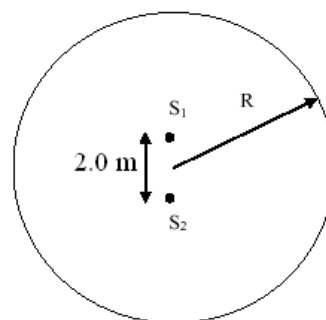


Figure 1

Ans:

$$\lambda = \frac{v}{f} = \frac{340}{680} = 0.50 \text{ m}$$

$$D = 2.0 \text{ m} \Rightarrow D = 4\lambda$$

\therefore The minima in the first quadrant correspond to: $\frac{\lambda}{2}, \frac{3\lambda}{2}, \frac{5\lambda}{2}, \frac{7\lambda}{2} \Rightarrow 4$ minima

\therefore On the big circle: $4 \times 4 = 16$ minima

Q6.

During a typical workday of eight hours, the average sound intensity arriving at a human ear is $1.8 \times 10^{-5} \text{ W/m}^2$. If the area of the human ear through which the sound passes is 2.1 cm^2 , what is the total energy entering each ear during the workday?

- A) $1.1 \times 10^{-4} \text{ J}$
- B) $1.8 \times 10^{-5} \text{ J}$
- C) $7.4 \times 10^{-4} \text{ J}$
- D) $4.1 \times 10^{-3} \text{ J}$
- E) $2.2 \times 10^{-4} \text{ J}$

Ans:

$$I = \frac{P}{A} \Rightarrow P = IA$$

$$E = P \cdot t = IA t = 1.8 \times 10^{-5} \times 2.1 \times 10^{-4} \times 8 \times 3600 = 1.1 \times 10^{-4} \text{ J}$$

Q7.

A tube closed at one end resonates in the standing wave pattern shown in **Figure 2**. If the length of the tube is 0.500 m, and the speed of sound in air is 343 m/s, what is the frequency of the emitted sound?

- A) 858 Hz
- B) 429 Hz
- C) 515 Hz
- D) 343 Hz
- E) 172 Hz



Figure 2

Ans:

The figure corresponds to the fifth mode ($n = 5$)

$$f_n = \frac{nv}{4L} \Rightarrow f_5 = \frac{5 \times 343}{4 \times 0.500} = 858 \text{ Hz}$$

Q8.

Two cars are traveling in opposite directions at the same speed when one of the drivers sounds the horn of his car, which has a frequency of 544 Hz. The other driver hears the frequency as 563 Hz. If the speed of sound in air is 344 m/s, what is the speed of the cars?

- A) 5.90 m/s
- B) 8.19 m/s
- C) 11.6 m/s
- D) 7.24 m/s
- E) 10.0 m/s

Ans:

$$f' = f \cdot \frac{v+x}{v-x} \quad \{x: \text{speed of cars}\} \quad \begin{array}{c} \text{S} \\ \ominus \rightarrow \end{array} \quad \begin{array}{c} \text{D} \\ \leftarrow \ominus \end{array}$$

$$\alpha = \frac{v+x}{v-x} \Rightarrow \alpha v - v = \alpha x + x \quad \left\{ \alpha = \frac{f'}{f} \right\}$$

$$\Rightarrow x = \frac{\alpha - 1}{\alpha + 1} \cdot v = \frac{1.04 - 1}{1.04 + 1} \times 344 = 5.90 \text{ m/s}$$

Q9.

At 20 °C, an aluminum cube has an edge length of 25 cm. What is the increase in the cube's total surface area when it is heated from 20 °C to 75 °C. The coefficient of linear expansion of aluminum is $23 \times 10^{-6}/\text{C}^\circ$.

- A) 9.5 cm²
- B) 1.6 cm²
- C) 6.3 cm²
- D) 13 cm²
- E) 4.7 cm²

Ans:

$$\text{One face: } \Delta A^* = 2 \alpha A \Delta T$$

$$\text{total: } \Delta A = 6 \Delta A^* = 12 \alpha A \Delta T$$

$$= 12 \times 23 \times 10^{-6} \times 625 \times 55 = 9.5 \text{ cm}^2$$

Q10.

A 0.0400-kg ice cube at 0.00 °C is placed in an insulated box that contains 0.0750 kg of water at 100 °C. What is the equilibrium temperature reached by this closed system?

- A) 37.6 °C
- B) 65.2 °C
- C) 50.7 °C
- D) 33.6 °C
- E) 22.7 °C

Ans:

$$Q_1 = m_i L_f = 0.04 \times 3.33 \times 10^5 = 13320 \text{ J}$$

$$Q_2 = m_i C_w \Delta T = 0.04 \times 4190 \times (T_f - 0) = 167.6 T_f$$

$$Q_3 = m_w C_w \Delta T = 0.075 \times 4190 \times (T_f - 100) = 314.25 T_f - 31425$$

$$Q_1 + Q_2 + Q_3 = 0: 481.85 T_f = 18105 \Rightarrow T_f = 37.6 \text{ °C}$$

Q 11.

A wall has a thickness of 0.61 m and a thermal conductivity of 2.1 W/(mC°). The temperature on one face of the wall is 3.2 °C, and 20.0 °C on the opposite face. How much heat is transferred in one hour through each square meter of the wall?

- A) $2.1 \times 10^5 \text{ J}$
- B) $7.7 \times 10^4 \text{ J}$
- C) 58 J
- D) $1.0 \times 10^5 \text{ J}$
- E) $1.8 \times 10^3 \text{ J}$

Ans:

$$P_{\text{Cond}} = \frac{k \cdot A \cdot \Delta T}{L} = \frac{2.1 \times 1.0 \times (20 - 3.2)}{0.61} = 57.8 \text{ W}$$

$$Q = P_{\text{Cond}} \cdot t = 57.8 \times 1 \times 3600$$

$$= 2.1 \times 10^5 \text{ J}$$

Q 12.

A system containing an ideal gas at a constant pressure of 1.22×10^5 Pa gains 2500 J of heat. During the process, the internal energy of the system increases by 2320 J. What is the change in the volume of the gas?

- A) $+1.48 \times 10^{-3} \text{ m}^3$
- B) $-1.48 \times 10^{-3} \text{ m}^3$
- C) $+3.66 \times 10^{-3} \text{ m}^3$
- D) zero
- E) $-3.66 \times 10^{-3} \text{ m}^3$

Ans:

$$\Delta E_{\text{int}} = Q - W$$

$$W = Q - \Delta E_{\text{int}}$$

$$P\Delta V = Q - \Delta E_{\text{int}}$$

$$\therefore \Delta V = \frac{Q - \Delta E_{\text{int}}}{P} = \frac{2500 - 2320}{1.22 \times 10^5} = +1.48 \times 10^{-3} \text{ m}^3$$

Q13.

Which one of the following properties of a gas is **NOT** consistent with the kinetic theory of gasses?

- A) The average speed of the gas molecules is smaller at higher temperatures.
- B) Gas molecules are widely separated.
- C) Gases fill whatever space is available to them.
- D) Gas molecules move rapidly in a random fashion.
- E) Gas molecules make elastic collisions with the walls of the container.

Ans:**A****Q14.**

A container having 150 kg of an ideal gas has a volume of 8.00 m^3 . If the gas exerts a pressure of 5.00×10^5 Pa, what is the rms speed of the molecules?

- A) 283 m/s
- B) 165 m/s
- C) 354 m/s
- D) 420 m/s
- E) 397 m/s

Ans:

$$v_{\text{rms}} = \sqrt{\frac{3RT}{M}} = \sqrt{\frac{3}{M} \cdot pV} = \sqrt{\frac{3pV}{M_{\text{Sample}}}}$$

$$= \sqrt{\frac{3 \times 5.00 \times 10^5 \times 8.00}{150}} = 283 \text{ m/s}$$

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Q17.

An ideal monatomic gas contains 5.00 moles. The pressure of the gas is doubled at constant volume. How much is the change in the entropy of the gas?

- A) + 43.2 J/K
- B) - 43.2 J/K
- C) - 72 J/K
- D) + 72 J/K
- E) zero

Ans:

$$\Delta S = \int \frac{dQ}{T} = \int \frac{nC_v dT}{T} = nC_v \ln\left(\frac{T_f}{T_i}\right) = n \cdot C_v \cdot \ln\left(\frac{P_f}{P_i}\right)$$

$$= 5.00 \times 1.5 \times 8.31 \times \ln(2) = + 43.2 \frac{\text{J}}{\text{K}}$$

Q18.

A heat engine operates between a hot reservoir at 1500 K and a cold reservoir at 500 K. During each cycle, 1.0×10^5 J of heat is removed from the hot reservoir and 5.0×10^4 J of work is performed. The actual efficiency of this engine is:

- A) 75 % of the maximum efficiency
- B) 67 % of the maximum efficiency
- C) 50 % of the maximum efficiency
- D) 17 % of the maximum efficiency
- E) 87 % of the maximum efficiency

Ans:

$$\epsilon_{\text{ideal}} = 1 - \frac{T_L}{T_M} = 1 - \frac{500}{1500} = \frac{2}{3}$$

$$\epsilon_{\text{real}} = \frac{W}{Q_H} = \frac{5.0 \times 10^4}{10 \times 10^4} = \frac{1}{2}$$

$$\frac{\epsilon_{\text{real}}}{\epsilon_{\text{ideal}}} = \frac{1}{2} \times \frac{3}{2} = \frac{3}{4} = 75\%$$

Q19.

A Carnot refrigerator is placed in a kitchen. The temperature inside the refrigerator is 2.0 °C, and the temperature of the kitchen is 22 °C. The rate of heat flow from the refrigerator to the kitchen is 24.7 kW. What power is needed to operate this refrigerator?

- A) 1.8 kW
- B) 3.6 kW
- C) 2.5 kW
- D) 4.7 kW
- E) 0.4 kW

Ans:

$$K = \frac{T_L}{T_H - T_L} = \frac{275.15}{22} = 13.75$$

$$K = \frac{Q_L}{W} \Rightarrow W = \frac{Q_L}{K} = \frac{24.7}{13.75} = 1.8 \text{ kW}$$

Q20.

A system consists of two thermal reservoirs in contact with each other, one at a temperature of 300 °C and the other at a temperature of 200 °C. If 6000 J of heat is transferred from the 300 °C reservoir to the 200 °C reservoir, what is the change in entropy of this system?

- A) +2.2 J/K
- B) +13 J/K
- C) -10 J/K
- D) +10 J/K
- E) -2.2 J/K

Ans:

$$\Delta S_1 = \frac{Q}{T_1} = +\frac{6000}{200 + 273} = +12.7 \frac{\text{J}}{\text{K}}$$

$$S_2 = \frac{Q}{T_2} = -\frac{6000}{300 + 273} = -10.5 \frac{\text{J}}{\text{K}}$$

$$\Rightarrow \Delta S = \Delta S_1 + \Delta S_2 = +2.2 \frac{\text{J}}{\text{K}}$$
