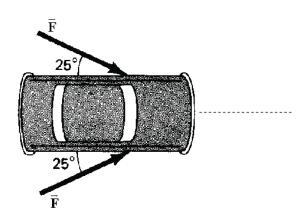
#### 3 December, 2011

Q1. Two persons pushed a car initially at rest at its front doors, each applying a force with magnitude  $|\vec{F}| = 300 \text{ N}$  at 25.0° to the forward direction, as shown in **Figure 1**. How much average power does **each person** requires in pushing the car 10.0 m for 10.0 seconds? Fig#



Answer:

 $W = 300 \times 10 \times \cos 25^{\circ} = 2719$  $P = W / t = \frac{300 \times 10 \times \cos 25^{\circ}}{10} = 271.8 \text{ W} \approx 272 \text{ W}$ 

A) 272 W
B) 145 W
C) 710 W
D) 424 W

E) 299 W

Q2. A spring has a spring constant k . If the work done in stretching the spring a distance x = L from the equilibrium position is W, the work required to stretch the spring from  $x_i = L$  to  $x_f = 2L$  will be:

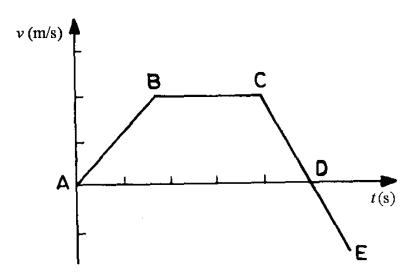
## Answer:

$$W = \frac{1}{2}k(L^{2} - 0) = \frac{1}{2}kL^{2}$$
$$W_{1} = \frac{1}{2}k\left[(2L)^{2} - L^{2}\right] = 3W$$

A) 3 W
B) 5 W
C) 4 W
D) 2 W

E) 1 W

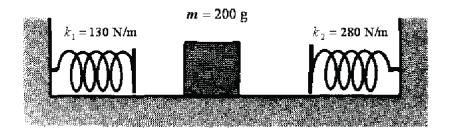
Q3. A single force acts on the body causing the body to move in a straight line. A plot of the body's velocity v (m/s) versus time t (s) is shown in the Fig 2. The **correct** statement among the following is: Fig#



A) in moving from D to E, the work done by the force on the body is positive.

- B) in moving from B to C no work is done on the body but the body does work on the system.
- C) in moving from C to D, the work done by the force on the body is positive.
- D) in moving from A to B, the work done by the force on the body is negative.
- E) in moving from A to D, the work done by the force on the body is positive.

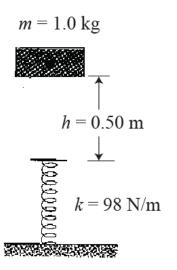
Q4. A block, of mass m = 200 g, slides back and forth on a **frictionless surface** between two springs, as shown in **Figure 3**. The left-hand side spring has  $k_1 = 130$  N/m and its maximum compression is 16 cm. The right-hand side spring has  $k_2 = 280$  N/m. Find the maximum compression of the right-hand side spring. Fig#



$$\frac{1}{2}k_{1}x_{1}^{2} = \frac{1}{2}k_{2}x_{2}^{2} \implies \frac{x_{2}^{2}}{x_{1}^{2}} = \frac{k_{1}}{k_{2}}$$
$$\implies x_{2} = \sqrt{\left(\frac{k_{1}}{k_{2}}\right)x_{1}^{2}} = \sqrt{\left\{\frac{130}{280}\right\}(16)^{2}} = 10.9 \text{ cm.}$$

A) 11 cm.
B) 14 cm.
C) 2.0 cm.
D) 30 cm.
E) 8.0 cm.

Q5. A block, of mass m = 1.0 kg, initially at rest, falls from a height of h = 0.50 m, on a vertical spring fastened to a horizontal board placed on the floor, as shown in **Figure 4**. If the spring constant is k = 98 N/m, the maximum compression that the spring undergoes is: Fig#



Answer:

$$mgh = mg(-x) + \frac{1}{2}kx^{2}$$
  

$$\Rightarrow 1.0g(0.5) = 1.0g(-x) + \frac{1}{2}(98)x^{2} \Rightarrow 1 = -2x + 10x^{2}$$
  

$$x = 0.43 \text{ m}$$

A) 0.43 m

- B) 0.17 mC) 0.34 mD) 0.86 m
- E) 0.54 m

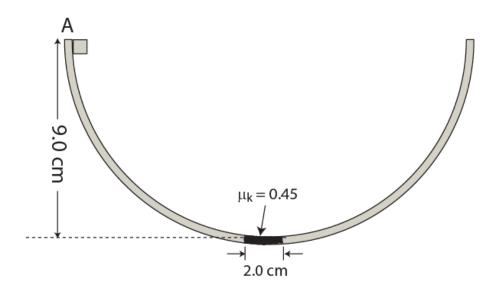
Q6. A single force F, of magnitude 10.0 N, accelerates an object of mass 5.00 kg for three seconds starting from rest at t = 0. What is the work done on the object in the time interval from t = 2.00 sec to t = 3.00 sec.

### **Answer:**

$$d_{3} - d_{2} = \frac{1}{2}a\left(3^{2} - 2^{2}\right) = 0 + \frac{1}{2}\frac{10}{5}5 = 5.00$$
$$\implies W = Fd = 10.0 \times 5.00 = 50.0 \text{ J}$$

- A) 50.0 J.
  B) 40.0 J.
  C) 20.0 J.
  D) 10.0 J.
- E) 25.0 J.

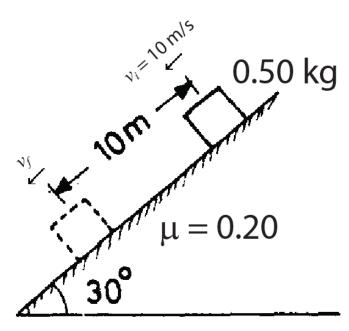
Q7. A block slides back and forth in a hemispherical bowl, starting from rest at the top point A, as shown in **Figure 5**. The bowl is frictionless except for a 2.0 cm-wide rough flat surface at the bottom, where coefficient of kinetic friction is  $\mu_k = 0.45$ . How many times does the block cross the rough region before coming to rest? Fig#



$$mgh = N \ \mu mgd \implies N = \frac{h}{\mu d} = \frac{9}{0.45 \times 2.0} = 10 \text{ times}$$

- A) 10 times.
- B) 14 times.
- C) 13 times.
- D) 3 times.
- E) 4 times.

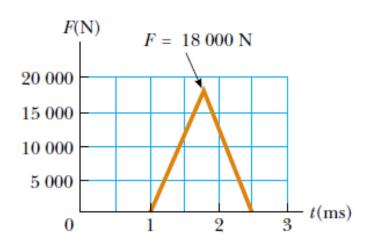
Q8. Figure 6 shows a block, of mass m = 0.50 kg with an initial speed of  $v_i = 10$  m/s, moving down an inclined rough plane of angle 30°. The coefficient of kinetic friction between the block and the plane is  $\mu = 0.20$ . The speed,  $v_f$ , of the block after it travels a distance of 10 m is: Fig#



$$\frac{1}{2}m(v_f^2 - 10^2) = (mg \sin 30^\circ - \mu mg \cos 30^\circ)d = mg(\sin 30^\circ - \mu \cos 30^\circ)10$$
  

$$\Rightarrow v_f^2 = 100 + 64.1 \Rightarrow v_f = \sqrt{164.1} = 12.8 \text{ m/s}$$
  
A) 13 m/s  
B) 24 m/s  
C) 8 m/s  
D) 17 m/s  
E) 36 m/s

Q9. A force F(t) (pointing in the + x-direction) acts on a ball with mass m = 0.060 kg initially at rest at t = 1.00 ms. Figure 7 shows a plot of F(t) vs t. Find the speed of the ball at t = 2.50 ms. Fig#



Answer:

$$p = \int F dt = \frac{1}{2} F dt$$
  
$$\Rightarrow v_f = \frac{1}{2} \frac{F dt}{m} = \frac{1}{2} \frac{18000 \times (2.5 - 1) \times 10^{-3}}{0.06} = 225 \text{ m/s}$$

A) 225 m/s
B) 375 m/s
C) 400 m/s

- D) 153 m/s
- E) 642 m/s

Q10. A system consists of two particles  $m_1$  and  $m_2$ , where the mass of  $m_2 = 0.10$  kg. At t = 0 s, the particle  $m_1$  was at  $x_1 = 0.0$  m and has a velocity  $\vec{v}_1$ , and the other particle  $m_2$  was at rest at  $x_2 = 8.0$  m. At t = 0 s, the center of mass of the system was at  $x_{com} = 2.0$  m, and has a velocity of  $\vec{v}_{com} = 5.0$  i m/s. What was the velocity  $\vec{v}_1$ ?

#### **Answer:**

All the velocities are in x-direction

Location of the center of mass system implies:

$$m_1 x_1 + m_2 x_2 = (m_1 + m_2) x_{cm} \implies 0 + 8 \times 1 = (m_1 + m_2) 2$$
 (1)

Velocity of the center of mass system implies

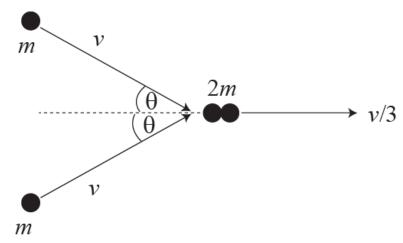
$$m_1 v_1 + m_2 v_2 = (m_1 + m_2) v_{cm} \implies m_1 v_1 = (m_1 + m_2) 5$$
 (2)

From (1) and (2) one finds:

 $m_1 = 0.3 \text{ kg}, \quad \vec{v}_1 = 6.7 \text{ i m/s}$ 

A)  $\vec{v}_1 = 6.7 \text{ i m/s}$ B)  $\vec{v}_1 = 2.7 \text{ i m/s}$ C)  $\vec{v}_1 = 1.8 \text{ i m/s}$ D)  $\vec{v}_1 = 3.4 \text{ j m/s}$ E)  $\vec{v}_1 = 9.2 \text{ i m/s}$ 

Q11. After a completely inelastic collision between two objects of equal mass *m*, each having an initial speed *v*, the two move off together with a speed v/3, see **Figure 8**. What was the angle (20) between their initial velocities? Fig#



#### Answer:

Conservation of momentum implies:

$$mv \cos\left(\frac{\theta}{2}\right) + mv \cos\left(\frac{\theta}{2}\right) = 2m\left(\frac{v}{3}\right)$$
  
 $\Rightarrow \theta = 2\cos^{-1}\left(\frac{1}{3}\right) = 141^{\circ}$ 

A)	141°
B)	134°
C)	102°
D	1(20

- D) 163°
- E) 127°

Q12. A ball of mass  $m_1$  makes a head on elastic collision with second ball, of mass  $m_2$ , initially at rest. If  $m_1$  rebounds in the opposite direction with a speed equal to one-fourth its original speed, what is the mass  $m_2$ ?

### Answer:

Conservation of momentum implies:

$$m_1 v_1 + 0 = m_1 \left(\frac{-v_1}{4}\right) + m_2 \left(\frac{3v_1}{4}\right)$$
$$\Rightarrow m_1 (1 + \frac{1}{4}) = \frac{3}{4} m_2 \Rightarrow \boxed{m_2 = \frac{5}{3} m_1}$$

A) 
$$\frac{5}{3}m_1$$
  
B)  $\frac{1}{2}m_1$   
C)  $\frac{1}{3}m_1$   
D)  $\frac{3}{4}m_1$   
E)  $\frac{7}{2}m_1$ 

Q13. A uniform disk of 1.0 m radius is rotating about its symmetry axis with a constant angular speed of 2.0 rad/s. What are the magnitude of the tangential acceleration  $a_t$  and centripetal acceleration  $a_r$  of a point on the rim of the disk?

$$\omega = 2 \text{ rad/s}, \text{ } r = 1 \text{ m},$$

$$a_r = \frac{v^2}{2} = r\omega^2 = 1 \times 2^2 = 4 \text{ m/s}^2,$$

$$a_t = \frac{d\omega}{dt} = 0$$
A)  $a_t = 0.0 \text{ m/s}^2, a_r = 4.0 \text{ m/s}^2$ 
B)  $a_t = 1.0 \text{ m/s}^2, a_r = 2.0 \text{ m/s}^2$ 
C)  $a_t = 0.0 \text{ m/s}^2, a_r = 1.0 \text{ m/s}^2$ 
D)  $a_t = 2.0 \text{ m/s}^2, a_r = 4.0 \text{ m/s}^2$ 
E)  $a_t = 4.0 \text{ m/s}^2, a_r = 0.0 \text{ m/s}^2$ 

Q14. A disk, subjected to a constant net torque, rotates around a fixed axis starting from rest. The ratio of work done by the torque during the (0 - 5.0 s) interval to the work done during the (5.0 s-10 s) interval is:

## Answer:

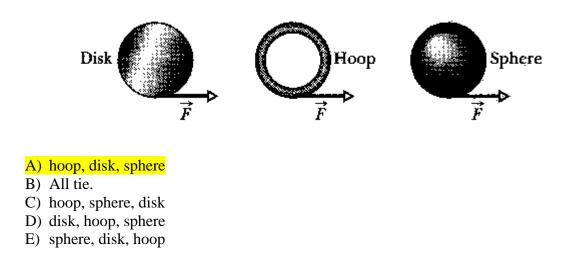
$$W = \tau \ \Delta\theta \Longrightarrow \frac{W_1}{W_2} = \frac{\Delta\theta_1}{\Delta\theta_2}$$
$$\Delta\theta_1 = 0 + 1/2 \ \alpha (5)^2 \quad \text{and} \ \Delta\theta_1 + \Delta\theta_2 = 0 + 1/2 \ \alpha (10)^2$$
$$\frac{W_1}{W_2} = \frac{\Delta\theta_1}{\Delta\theta_2} = \frac{25}{75} = \frac{1}{3}$$

A) 1/3
B) 1/2
C) 3
D) 2

- D) 2
- E) 4

Q15. A uniform disk, a thin hoop, and a uniform solid sphere, all with the same mass and same outer radius, are each free to rotate about a fixed axis through their centers. Identical forces are simultaneously applied to the rims of the objects, as shown in **Figure 9**. If the objects start from rest, rank the objects according to their angular speeds achieved after a given time (*t* sec), **least to greatest**.

Fig#



Q16. An engine applies a constant torque of 5.00 N·m on a wheel, with moment of inertia  $I_0 = 10.0 \text{ kg.m}^2$ , to rotate it about its symmetry axis O. How much power is required by the engine to rotate the wheel at t = 5.00 s, if the wheel starts from rest? Answer:

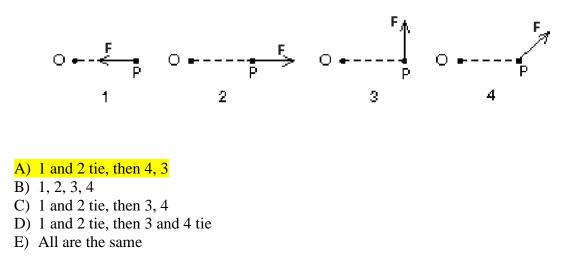
$$P_{av} = \vec{\tau} \cdot \vec{\omega} = \tau \alpha t = \frac{\tau^2 t}{I} = \frac{5^2 \times 5}{10} = 12.5 \text{ W}.$$

A) 12.5 W
B) 3.06 W
C) 6.20 W
D) 2.53 W

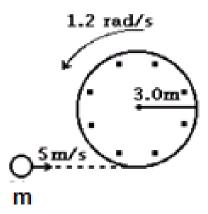
D) 2.35 W

E) 1.62 W

Q17. A single force **F** acts on a particle P. Rank each of the orientations of the force shown in **Figure 10** according to the magnitude of the time rate of change of the particle's angular momentum about the point O, **least to greatest**. Fig#



Q18. A disk with radius of 3.0 m and a moment of inertia of  $8000 \text{ kg} \cdot \text{m}^2$  is rotating about its central axis without friction with an angular velocity of 1.2 rad/s. Initially a man with mass **m** is moving with a velocity of 5.0 m/s, on a line tangent to the edge of the disk, as shown in **Figure 11**. The man jumps onto the edge of the disk. The final angular velocity of the disk and the man is 1.24 rad/s. The mass of the man **m** is: Fig#



# Answer:

Conservation of angular momentum implies:

$$I_{1}\omega_{1} + mvr = I_{1}\omega_{1} + mr^{2}\omega$$
  

$$\Rightarrow I_{1}(\underbrace{1.2 - 1.24}_{-0.04}) = m_{1}(r^{2}\omega - vr) = m(3)(3 \times 1.24 - 5) = 3m(-1.28)$$
  

$$\Rightarrow m = \frac{8000 \times 0.04}{3 \times 1.28} = 83.3 \text{ kg}$$
  
A) 83 kg  
B) 61 kg  
C) 75 kg  
D) 53 kg

E) 94 kg

Q19. A disk starts from rest and rotates with a constant angular acceleration. If the angular velocity is  $\omega$  rad/s at the end of the first two revolutions, then at the end of the first eight revolutions, the angular velocity will be:

## Answer:

$$\omega^{2} = \omega_{0}^{2} + 2\alpha \ \Delta\theta$$
  

$$\omega_{2}^{2} = 0 + 2\alpha (2 \times 2\pi) \text{ and } \omega_{8}^{2} = 0 + 2\alpha (8 \times 2\pi)$$
  

$$\frac{\omega_{2}^{2}}{\omega_{8}^{2}} = \frac{2}{8} \implies \frac{\omega_{2}}{\omega_{8}} = \frac{1}{2} \implies \omega_{8} = 2\omega_{2} = 2\omega \text{ rad/s}$$

## A) 2 ω rad/s

B)  $\sqrt{2} \omega \text{ rad/s}$ 

C)  $3 \omega \text{ rad/s}$ 

3 December, 2011

D) 4  $\omega$  rad/s

E) 5  $\omega$  rad/s

Q20. A hoop rolls without sliding along a horizontal floor. The ratio of its translational kinetic energy to its rotational kinetic energy (about an axis through its center of mass) is: **Answer:** 

$$K_{r} = \frac{1}{2}I\omega^{2}, K_{t} = \frac{1}{2}mv^{2} = \frac{1}{2}mr^{2}\frac{v^{2}}{r^{2}} = \frac{1}{2}I\omega^{2}$$
$$\Rightarrow \frac{K_{t}}{K_{r}} = 1.$$

A) 1

B) 2

C) 3

Ď) 1/2

E) 1/3